

Molecular Rayleigh scattering to measure fluctuations in density, velocity and temperature in wind tunnel applications (Phase I)

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Goal

To advance Rayleigh scattering based measurement technique for application in wind tunnel environment

- Setup proof of concept systems to learn and overcome difficulties in wind tunnel applications
- Simultaneous measurements of fluctuations in velocity, temperature and density - up to 25kHz bandwidth



Motivation

- Every wind-tunnel needs to know the level of free-stream turbulent fluctuations
Do the existing transonic, supersonic, hypersonic wind tunnel know that number?
Perhaps not.
- Lack of measurement tools for high speed flows
 - Need scalars T , ρ , P in addition to velocity \mathbf{U}
 - Existing tools cannot measure fluctuations in T , ρ
 - PIV, LDV, hot-wire primarily measures \mathbf{U}
 - Cannot measure turbulent stress: $\rho u u$, $\rho v v$ etc; needs simultaneous measurement of ρ & \mathbf{U}
- Experimental data on shock-waves and their unsteadiness hardly exist.
- Critical parameters for CFD validation, aero-acoustic modelling, heat- and mass transfer modelling cannot be measured.
 - ρ - U , T - U correlations, pressure-strain correlations etc
 - Frequency-wavenumber spectra of fluctuations in T , ρ , $\rho u u$

Existing/ past Rayleigh efforts:

- A. GRC/Universities - Jet noise source identification, heated and unheated transonic & supersonic jets
- B. Studies of premixed H_2 - O_2 flame etc.

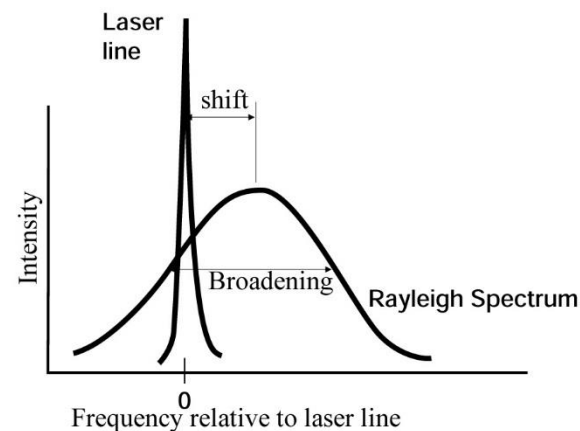
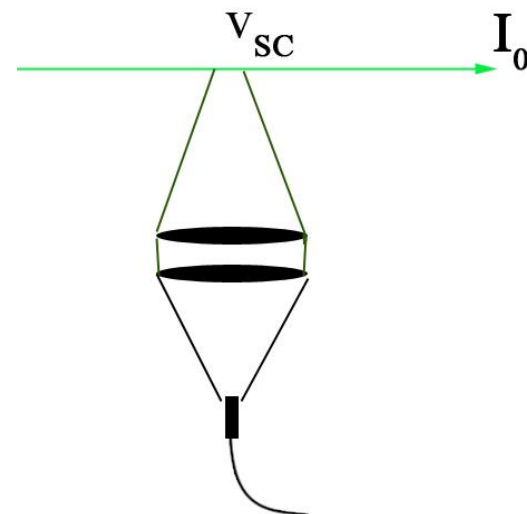


Presentation Roadmap:

- Basics of aerodynamic measurement using Rayleigh scattering
- Basics of air density measurement
- Bench-top setup created in the Fluid Mechanics Lab
- Measurement of density fluctuations spectra in a heated plume
- Basics of velocity and temperature measurement
- Setup of a spectroscope – progress made so far.
- Rayleigh setup in a low-speed Wind tunnel
Application –boundary layer transition observed via density fluctuations
- Summary, Deliverable, Schedule

Basics: Aerodynamic Measurements via Molecular Rayleigh scattering of Laser light

- A particle-free, non-intrusive technique to simultaneously measure density, temperature & velocity
- A laser beam is passed through the air-stream & light scattered by O_2 and N_2 molecules from points along the beam are collected and analyzed
- Air density from molecular num density
 - Requires measurement of light intensity
- Air velocity from the shift in the spectral peak.
 - Requires high-resolution spectral analysis of scattered light
 - Needs single-mode laser
- Air temperature from the width of the distribution of molecular speed.



Density measurement using Rayleigh Scattering

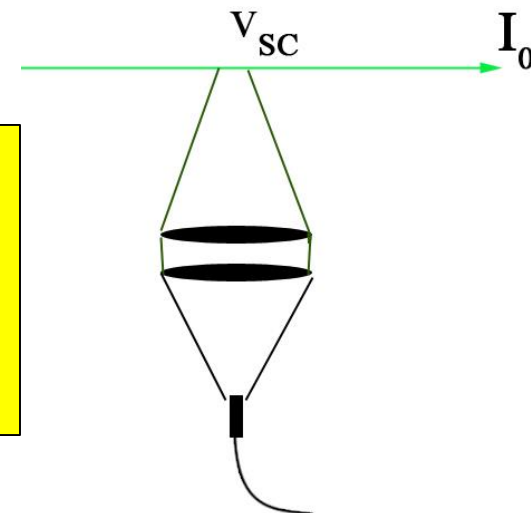
Power of scattered light $P_s = m I_0 V_{sc} \left(\sum_i \mu_i \frac{\partial \sigma_i}{\partial \Omega} \right) \sin^2 \chi d\Omega$

m molecular no density
 I_0 Incident Light irradiance
 V_{sc} Probe volume
 $\left(\sum_i \mu_i \frac{\partial \sigma_i}{\partial \Omega} \right)$ Scattering cross-section
 $\sin^2 \chi$ Angle from polarization plane
 $d\Omega$ Collection solid angle

$$m = \frac{\rho N_A}{M}$$

of photoelectrons $N = \frac{\epsilon \rho N_A I_0 V_{sc} \left(\sum_i \mu_i \frac{\partial \sigma_i}{\partial \Omega} \right) \sin^2 \chi d\Omega \Delta t}{M h \nu} = k \rho \Delta t$

- In absence of dust particles, in a constant composition gas mixture (air), the intensity of total scattered light is proportional to the local density
- Fluctuations in light intensity ~ fluctuations in air density





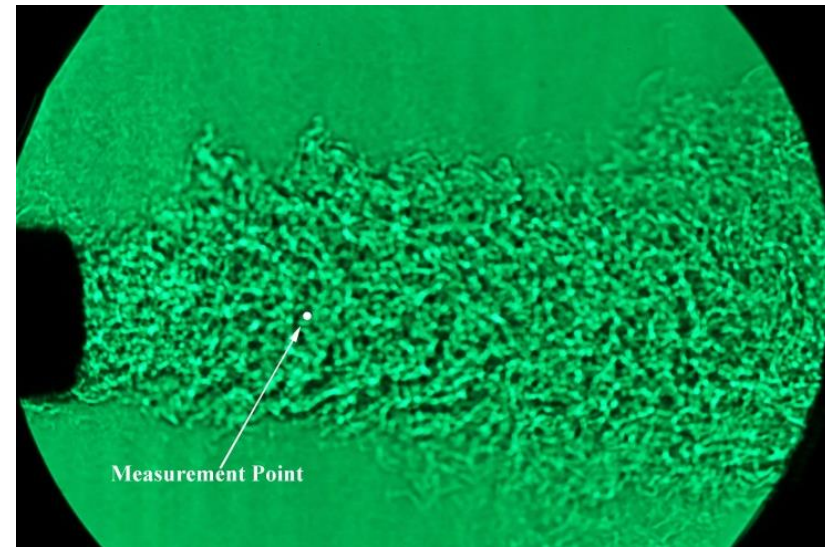
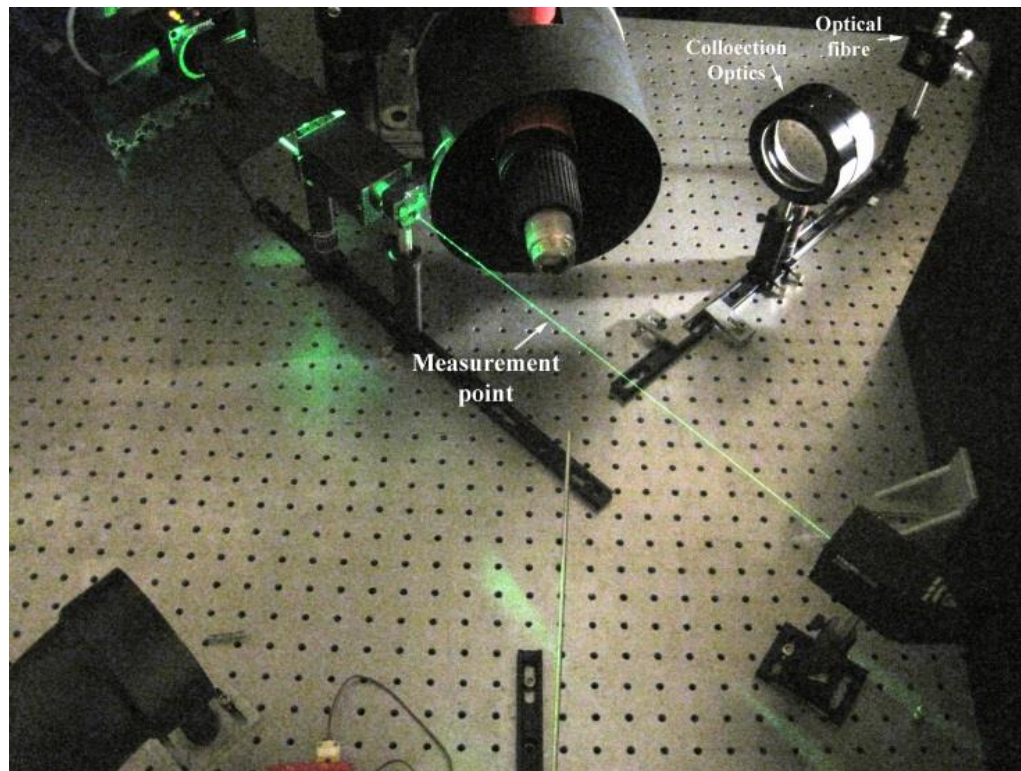
Challenges with implementation:

- Efficient removal of dust particles
 - Rayleigh scattering cross-section at ambient condition:
 $\sigma (\text{N}_2) = 5 \times 10^{-32} \text{ m}^2$; $\sim 10^{15}$ molecules in probe vol
Total scattering cross-section = $5 \times 10^{-17} \text{ m}^2$
 - σ (1 micron water droplet) $\sim 10^{-16} \text{ m}^2$

Scattering from a single 1 micron particle
is stronger than the total molecular scattering

- Very low light intensity – photon counting and shot noise
- Suppression of background light
- Vibration isolation
- Design application specific optical setup

Bench top setup in a low speed hot plume

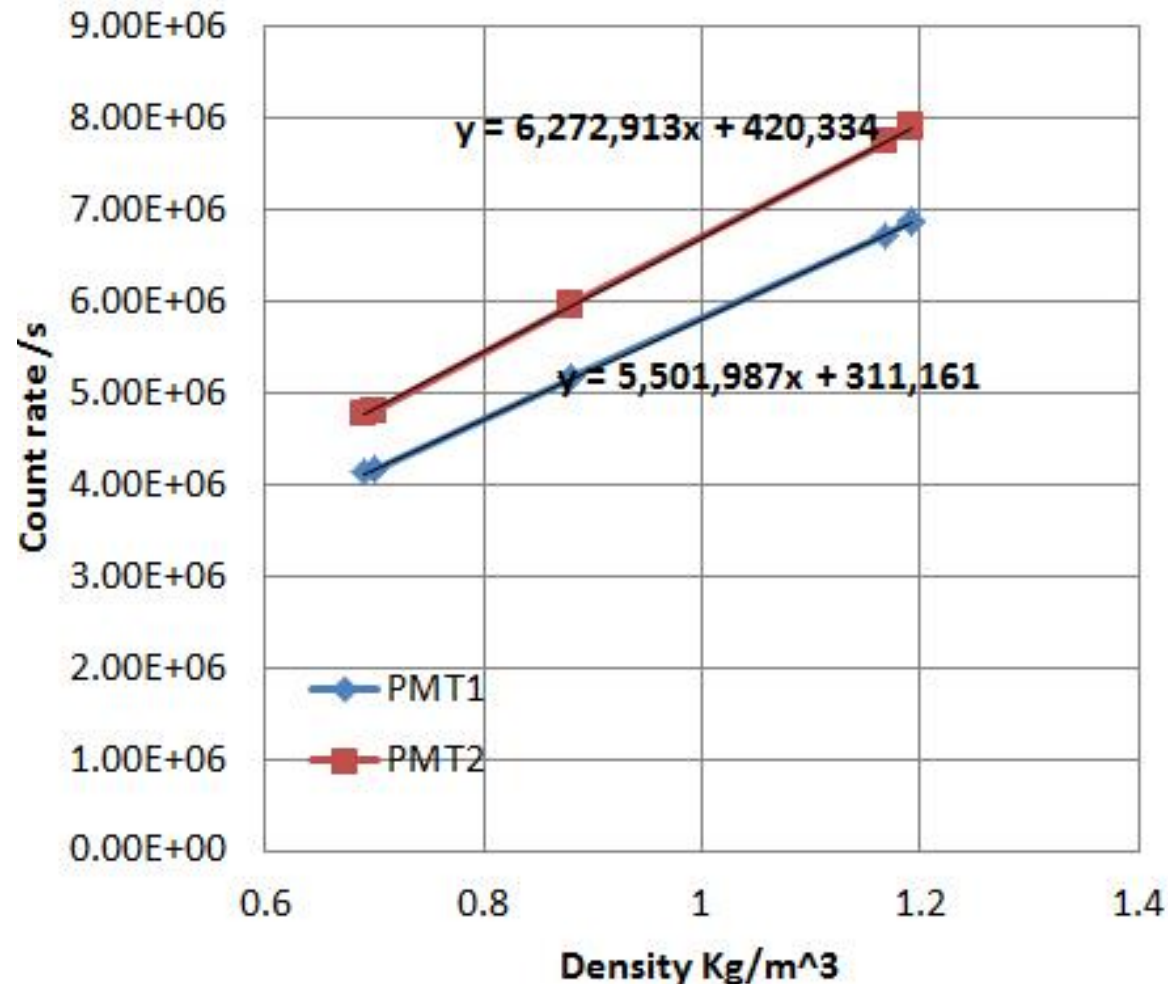


Shadowgraph of hot-plume and location of the probe volume

- Air flow cleaned by a HEPA filter
- Center hot plume from an electric heater
- Laser: Nd:VO₄ freq doubled to 532nm, CW, 2W
- f/4 collection optics
- 0.6 mm long probe volume along laser path

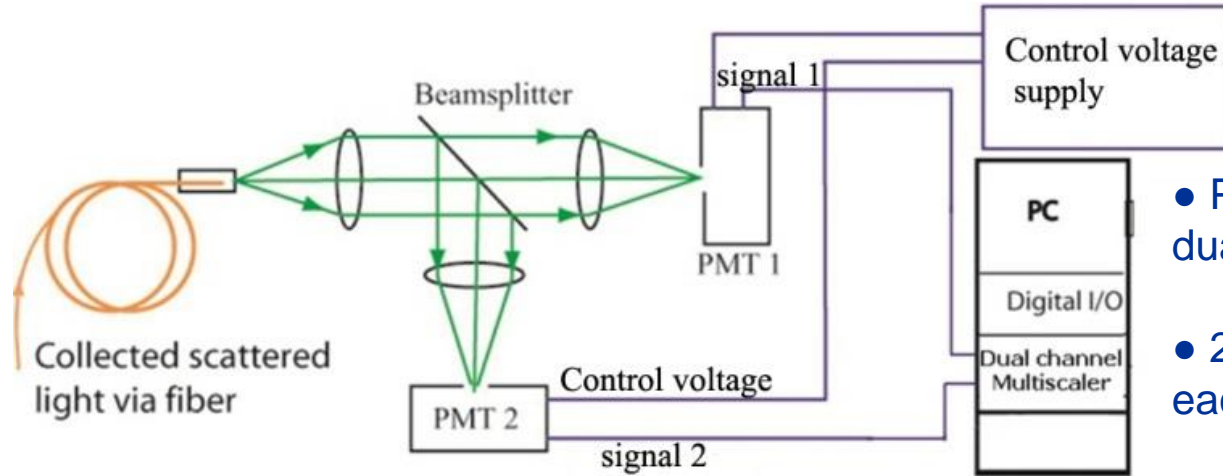
Density measurement

Calibration: count rate vs density, hot-plume setup



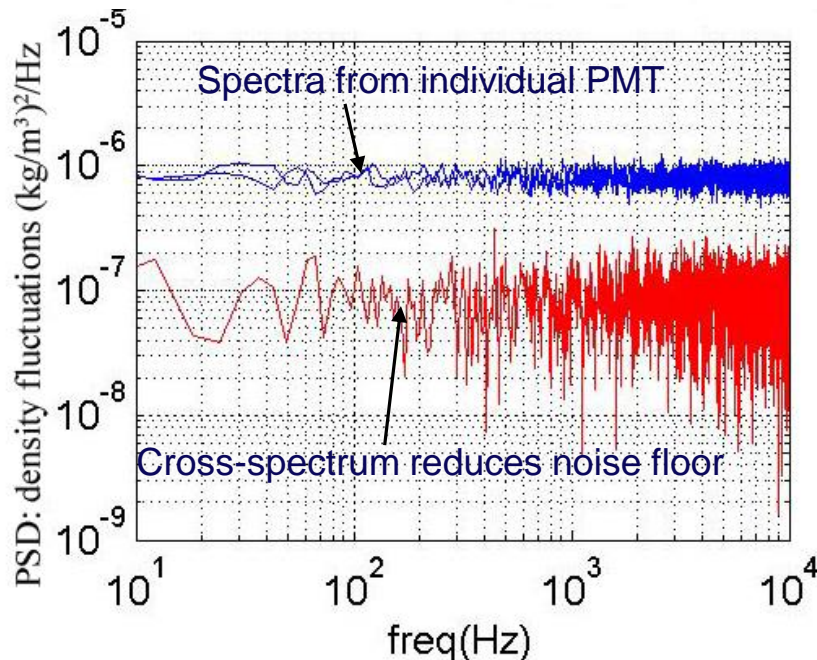
$$N_{av} = (a \rho + b) \Delta t, \quad \text{where } N_{av} = \frac{\sum N_i}{n}$$

Reduction of Electronic shot noise via 2-PMT cross-correlation technique



- Photo-electron counting using dual channel multi-scalar

- 262144 contiguous time bins each 20 to 50μ-s duration



Electronic shot noise is the primary source of uncertainty in spectral data

- Minimization using cross spectral density:

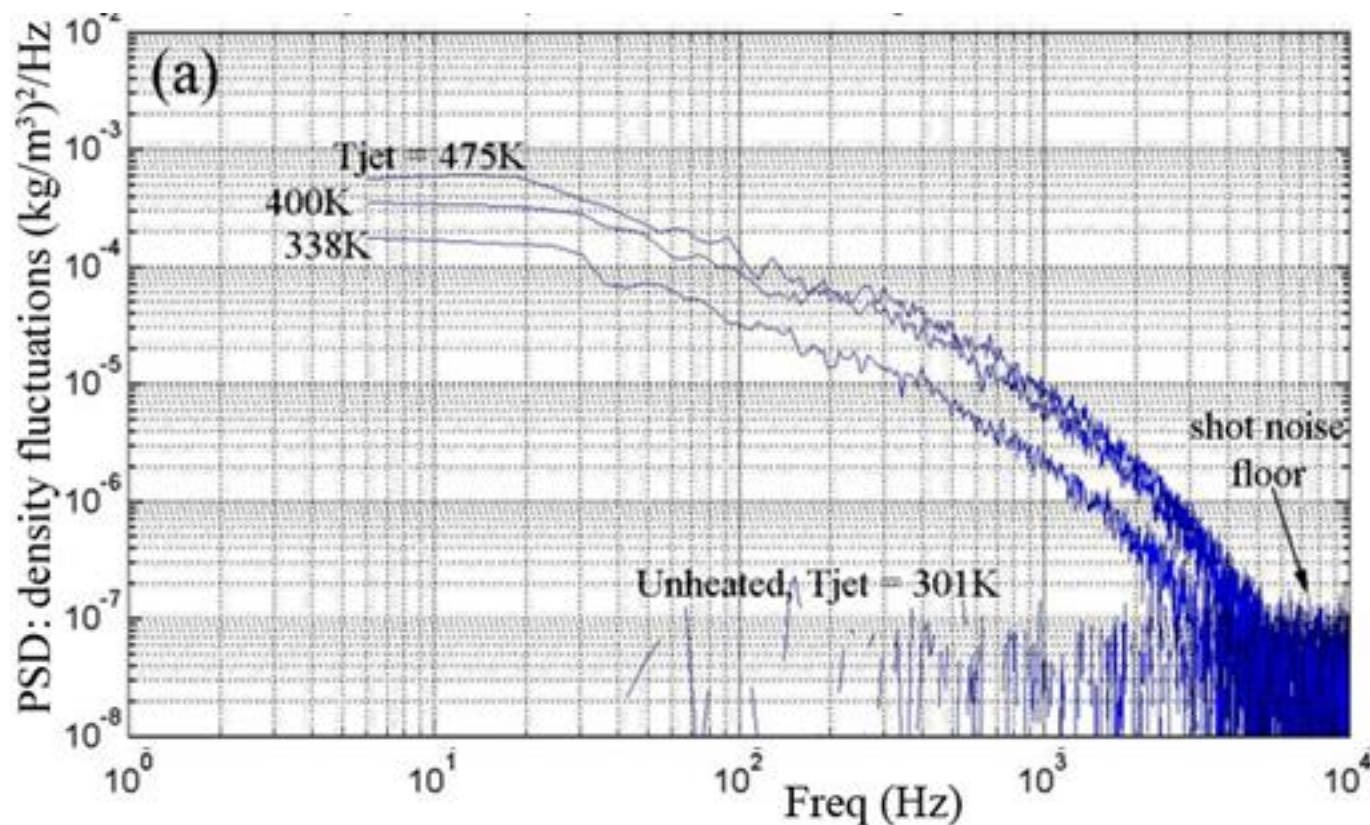
$$\left| P_{N'_1 N'_2}(f_l) \right| = \frac{2}{n^2} \left| F_{N'_1}(l) \cdot F_{N'_2}^*(l) \right|,$$

- Density fluctuations spectra:

$$P_{\rho'^2}(f_l) = \frac{\left| P_{N'_1 N'_2}(f_l) \right|}{a_1 a_2 (\Delta t)^2}$$

Spectra from ambient (no fluctuations in density) air

Density fluctuations spectra from hot plume of bench-top setup



- Spectra from plume centerline at indicated Temperatures
- **Excellent signal to noise ratio $>10^4$**

Measurement of Velocity and Temperature via Spectroscopic Analysis of Scattered Light

- Gas molecules in an airstream flowing with velocity U have a distribution of velocity, such as:

$$f(V)d^3V = \frac{n}{\pi^{3/2}a^3} \exp\left(-\frac{(V-U)^2}{a^2}\right) d^3V$$

$$a = \left(\frac{2k_B T}{m}\right)^{1/2}, \quad T = \text{gas Temperature}$$

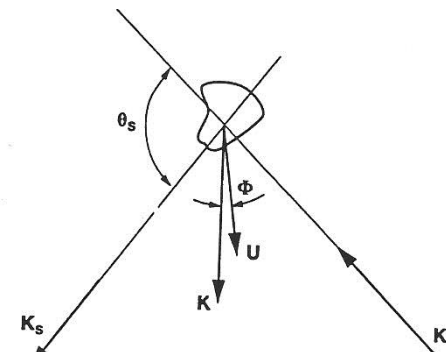
- Which manifests as a distribution of Doppler shift of incident light

$$f_d = \frac{k \cdot U}{2\pi}$$

- High resolution Fabry-Perot interferometer is used to measure Doppler shift.
- The Measured spectrum is a convolution of instrument function $I(\nu')$ and Rayleigh Spectrum $S_R(\nu - \nu')$

$$S_M(\nu) = G_R \int I(\nu') S_R(\nu - \nu') d\nu'$$

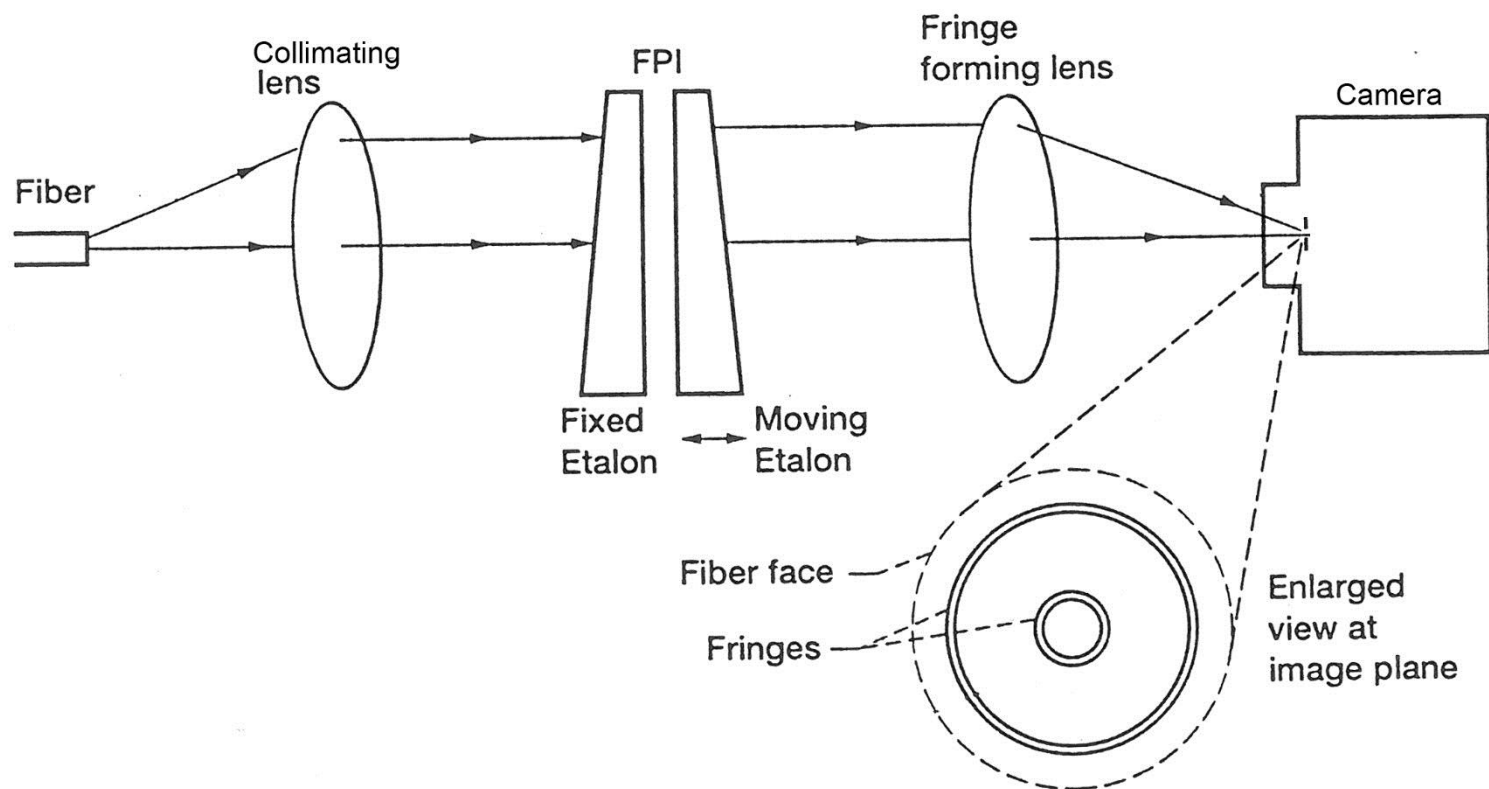
- Significant modelling is required to extract velocity and temperature from Rayleigh spectrum



Scattering diagram to measure velocity

Measurement of Velocity and Temperature via Spectroscopic Analysis of Scattered Light

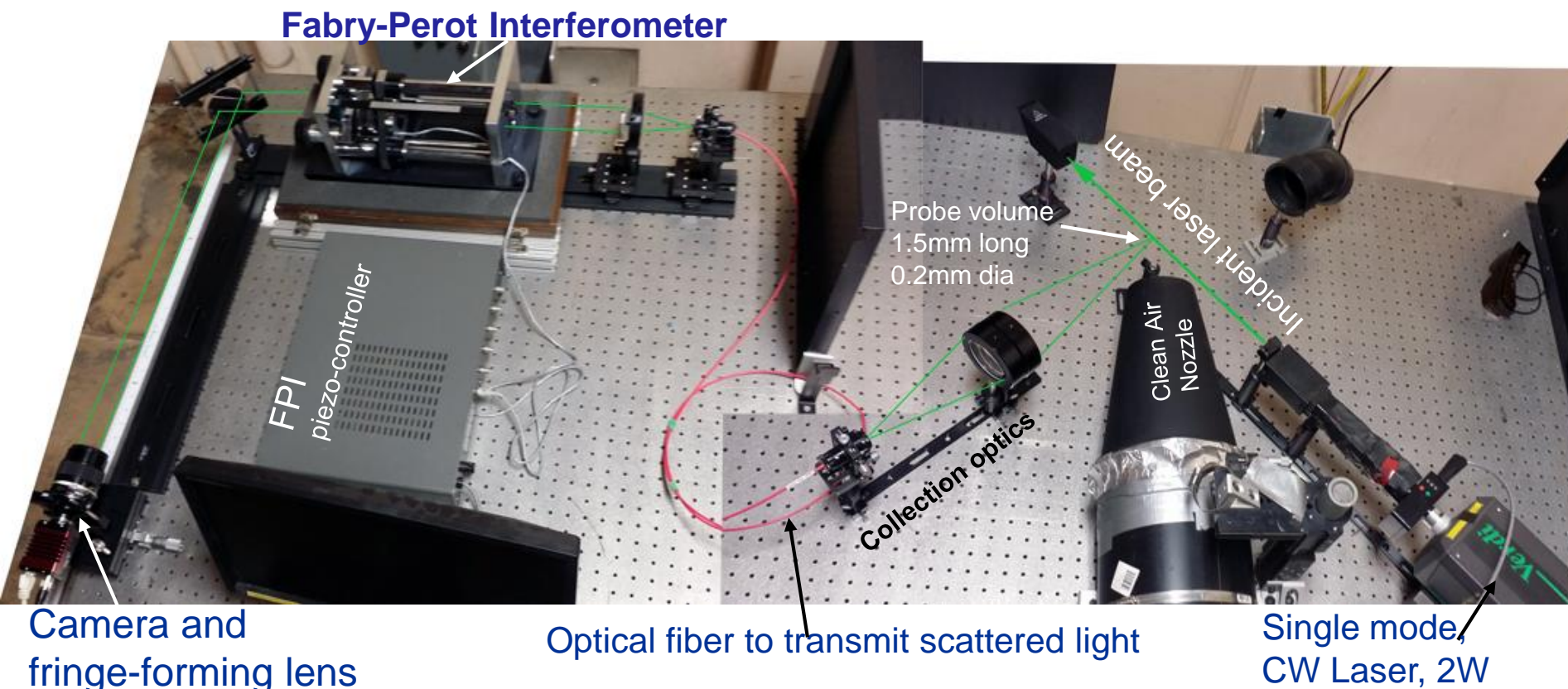
Fabry-Perot acts as a frequency dependent light filter



Fabry-Perot interferometer to spectrally resolve Rayleigh scattered light

- High resolution: FPI free-spectral range set to 7.5GHz

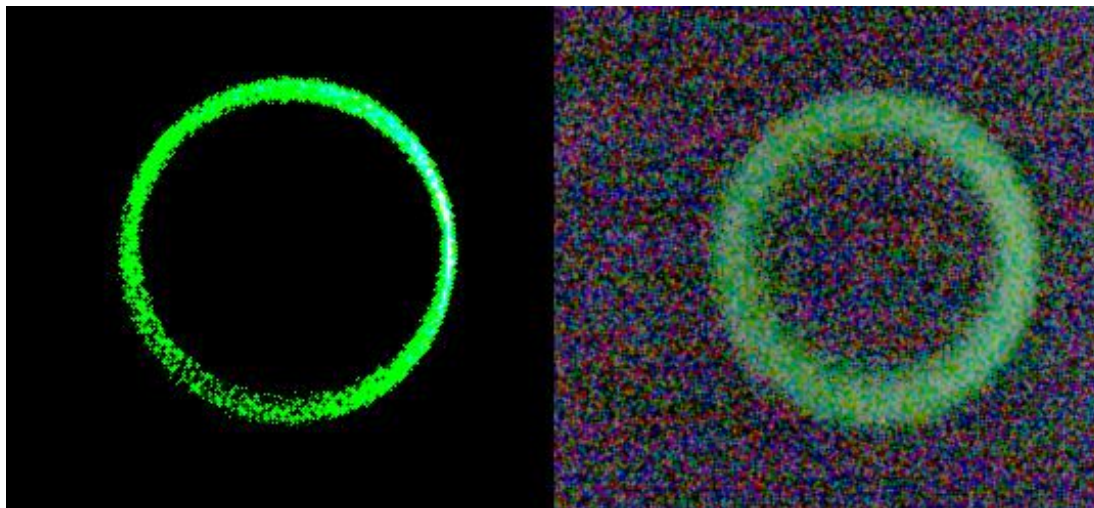
Spectroscopic setup to measure Velocity and Temperature



Setup at FML Test Cell I

- All optics (except Laser) and electronics were purchased using seedling fund

Spectroscopic setup to measure Velocity and Temperature



Reference spectrum
of incident laser

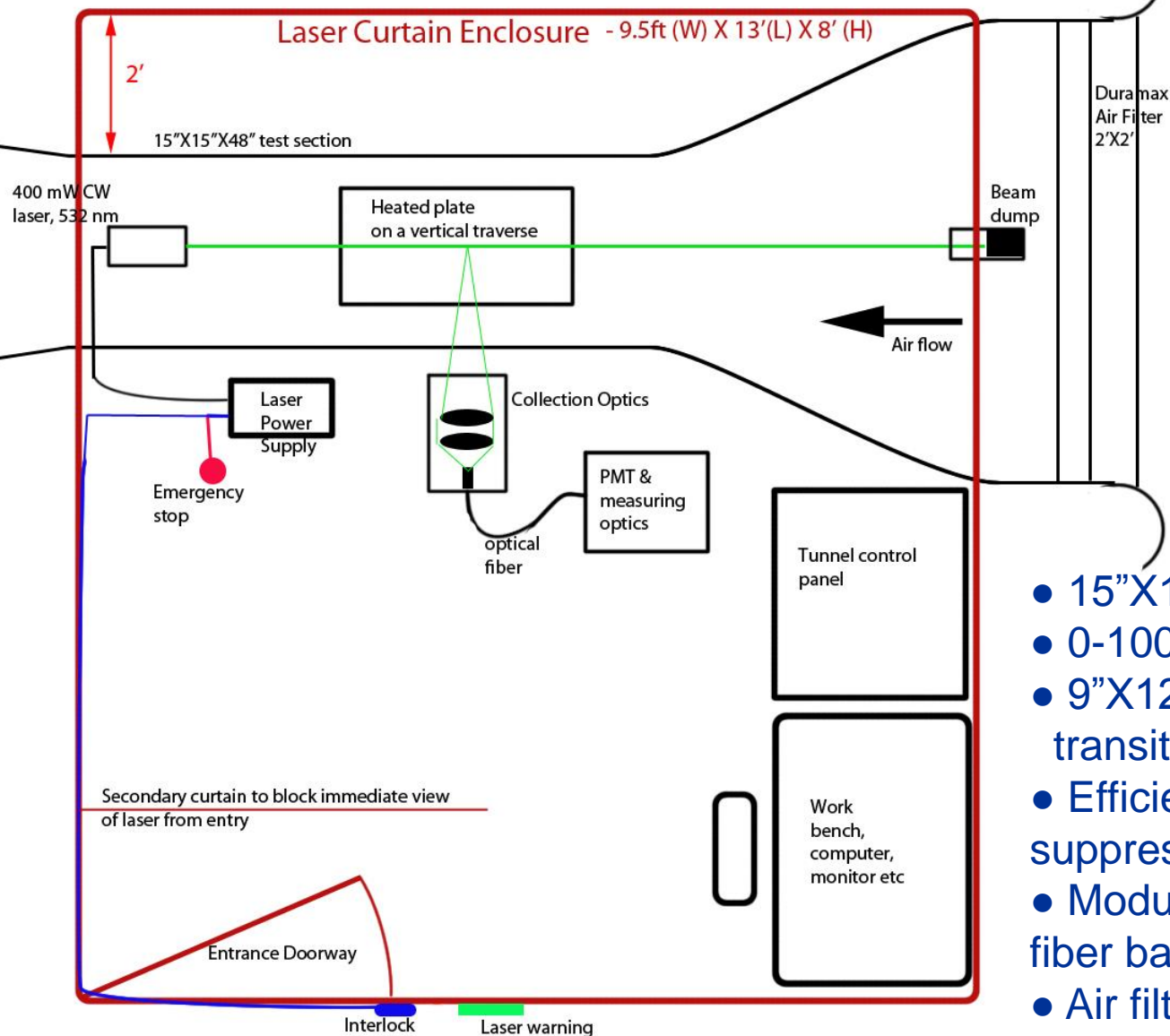
Spectrum of **Rayleigh scattered light**
• Fairly noisy

Work in progress - future work:

1. Buy /borrow low noise (cooled), high-speed camera
2. Software to establish Rayleigh spectra from optical fringes – big job!
3. Stabilization of Fabry-Perot
4. Measure time-average Rayleigh spectra – Time averaged U, T
5. Measure unsteady Rayleigh spectra – Fluctuating U, T

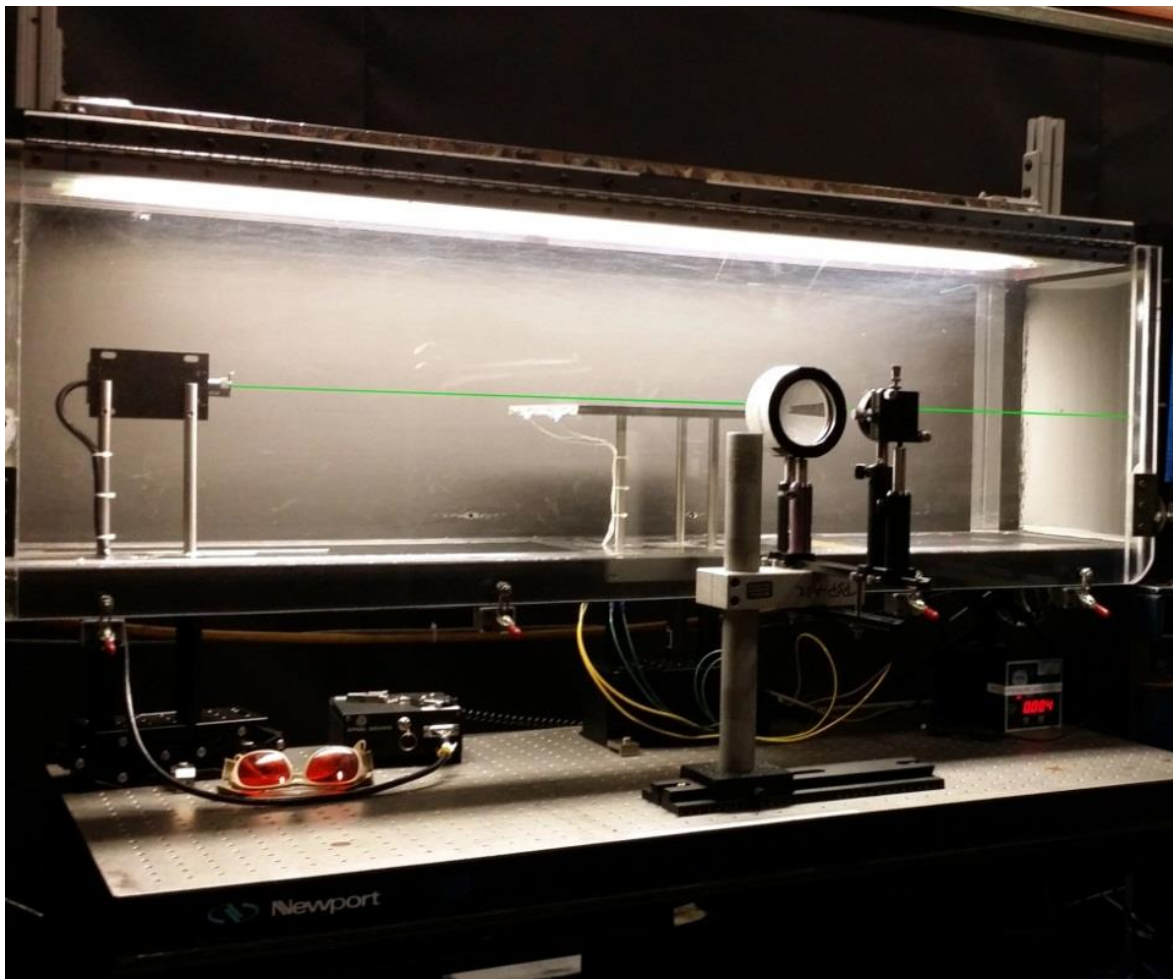


Rayleigh scattering setup in the FML "blue wind tunnel"



- 15"X15"X48" test section
- 0-100 ft/s flow
- 9"X12" heated flat plate for transition study
- Efficient background suppression
- Modular design – optical fiber based
- Air filtration at inlet

Setup in a Low-speed wind tunnel



Setup to study boundary-layer transition over a heated plate



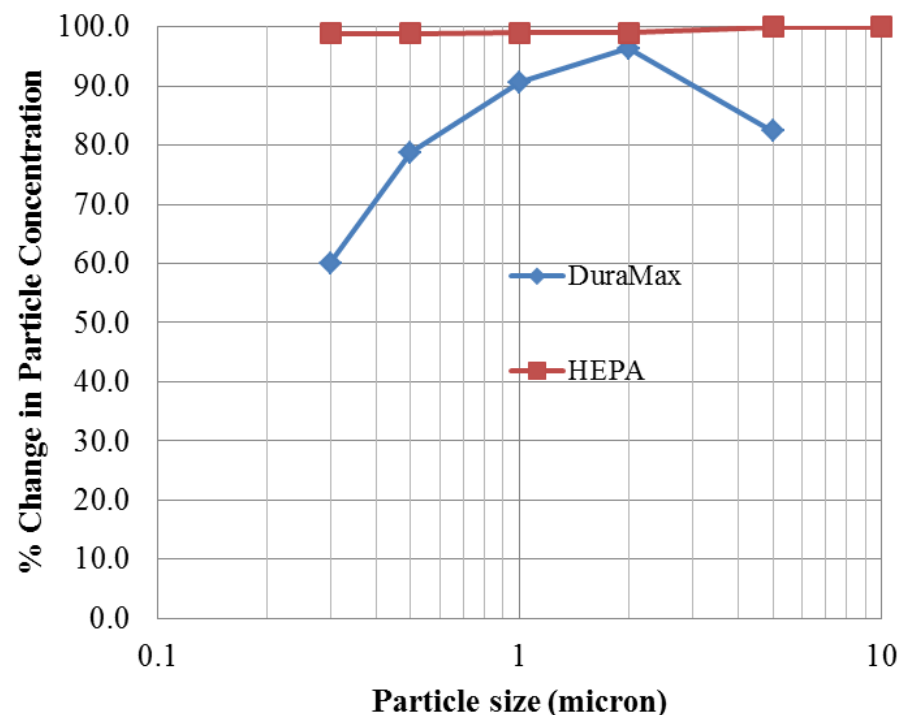
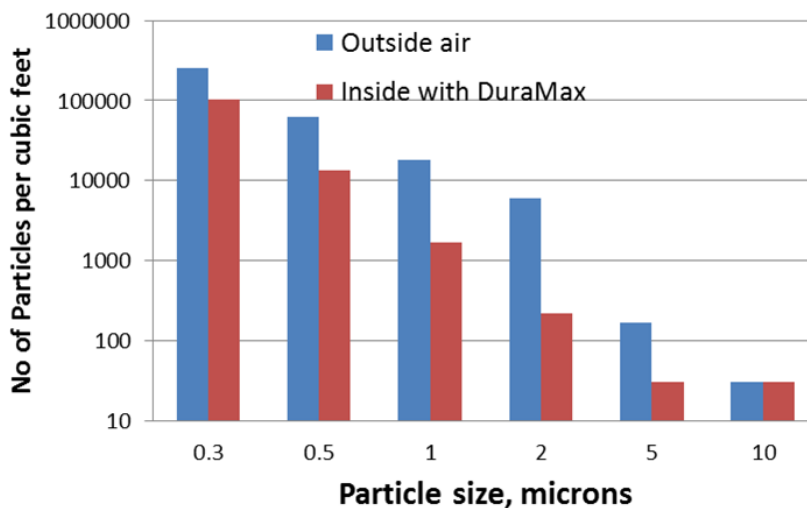
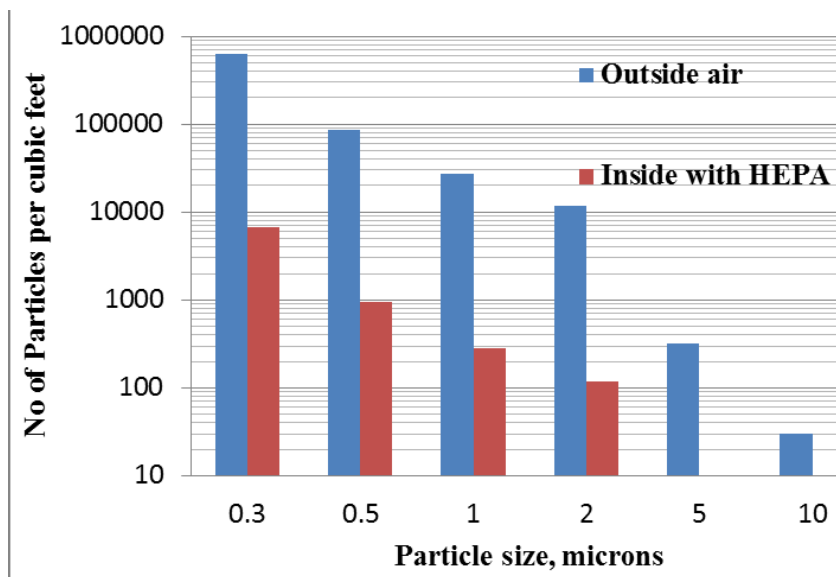
Air filter at tunnel inlet for dust removal

- airflow restriction
- Large filter-box for higher speed.



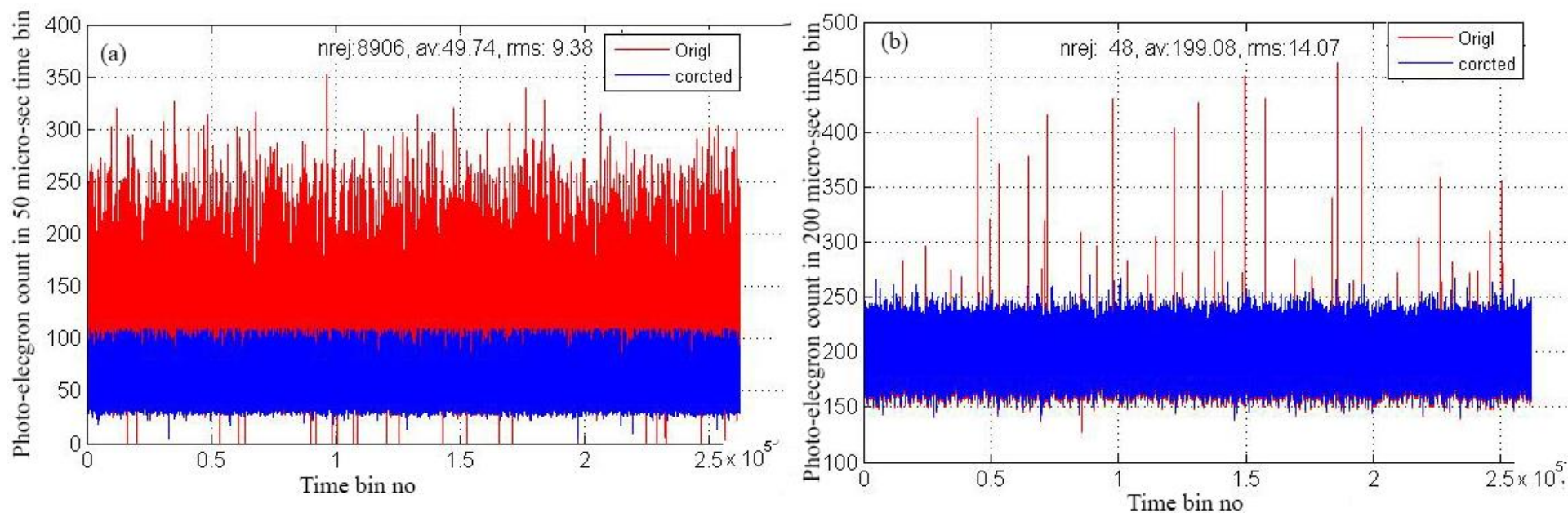
Dust removal from wind tunnel air stream

Measurement of particle concentration

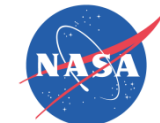


- Experimentation with different types of air filters were
- HEPA filters provide sufficient cleaning

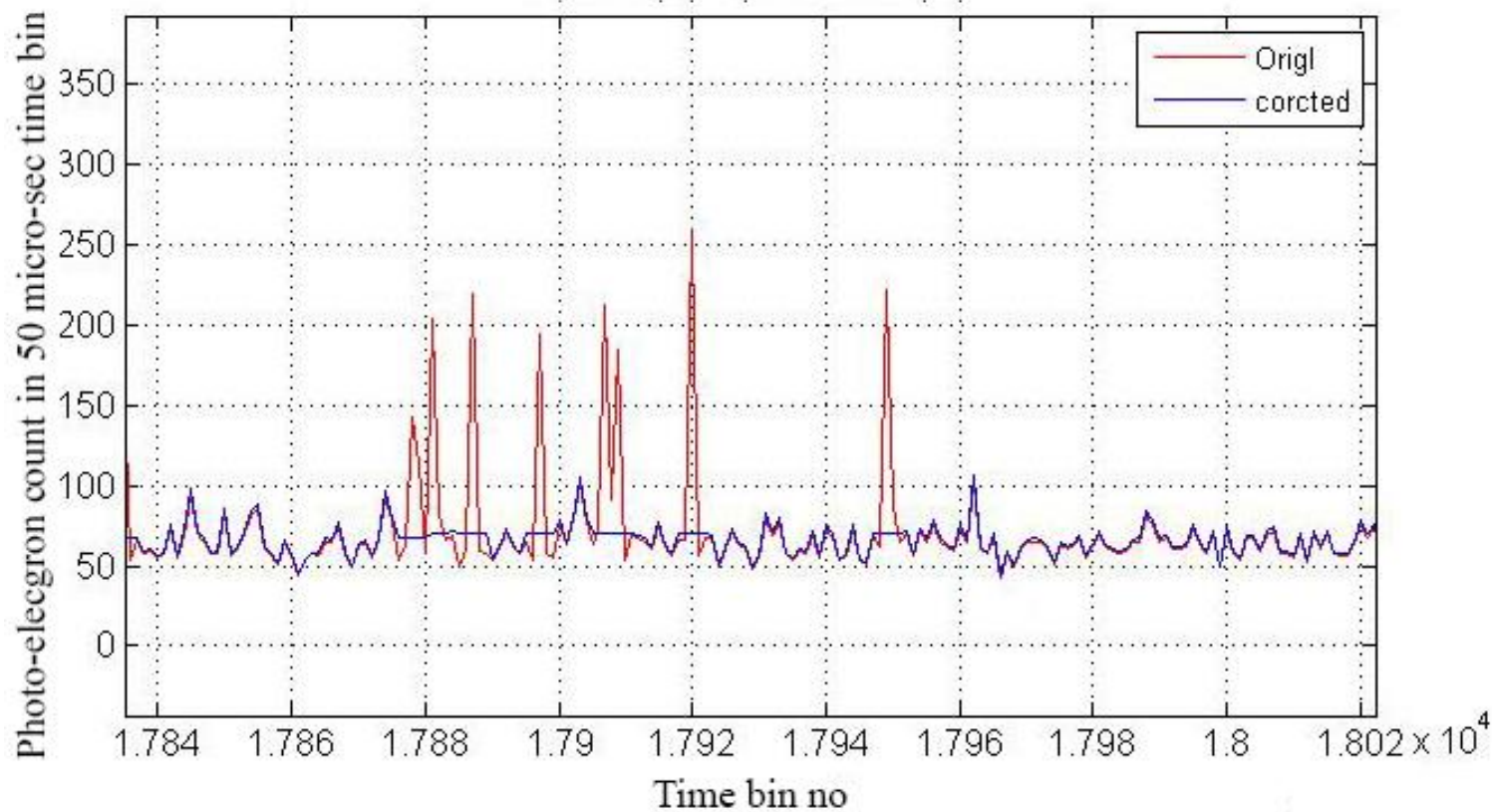
Impact of Dust Particles on Rayleigh Signature



Software Removal of Particle Signature

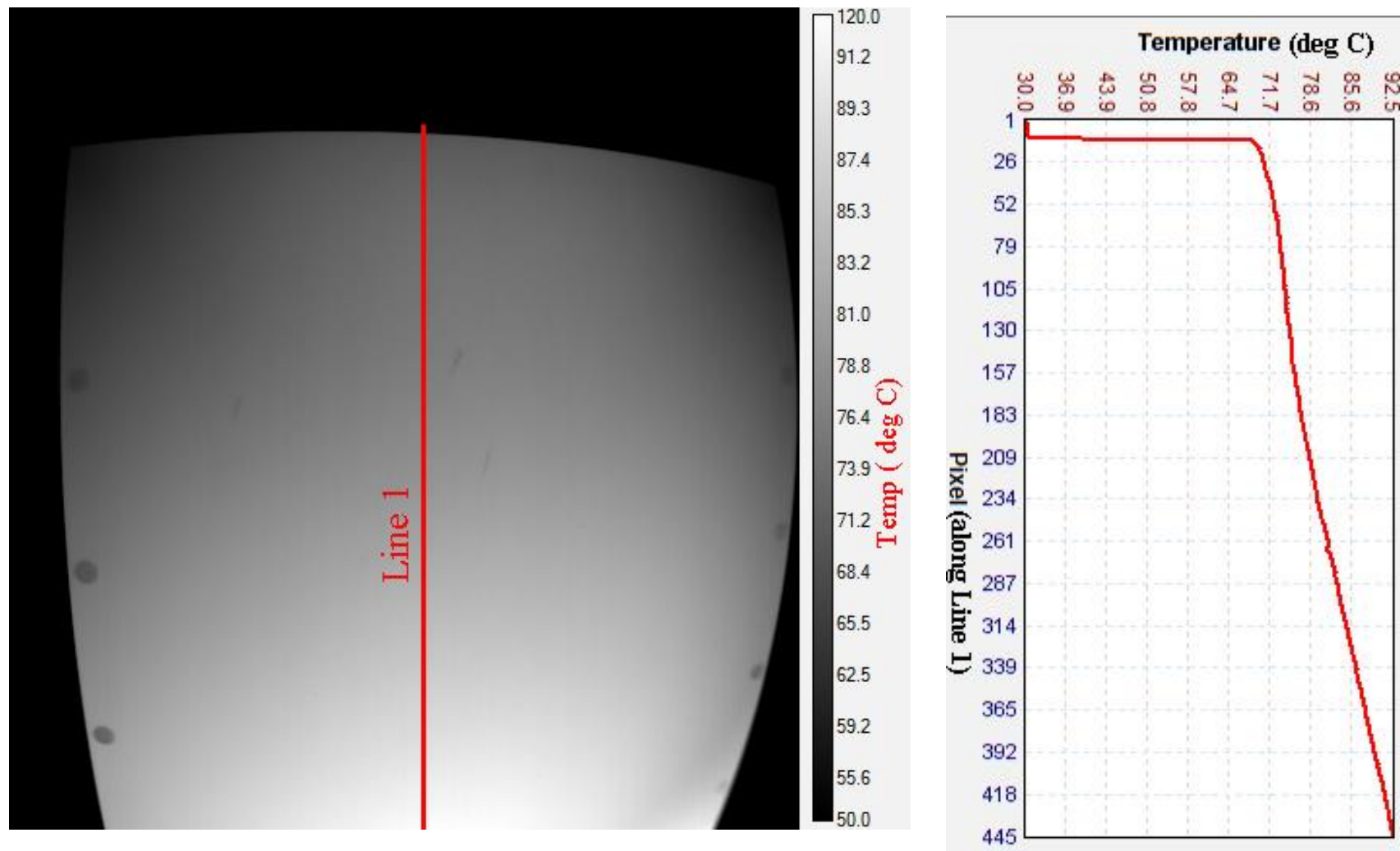


$$\text{If } N_i \geq kN_{stddev} \text{ } N_i = N_{av}, \quad k = 5$$



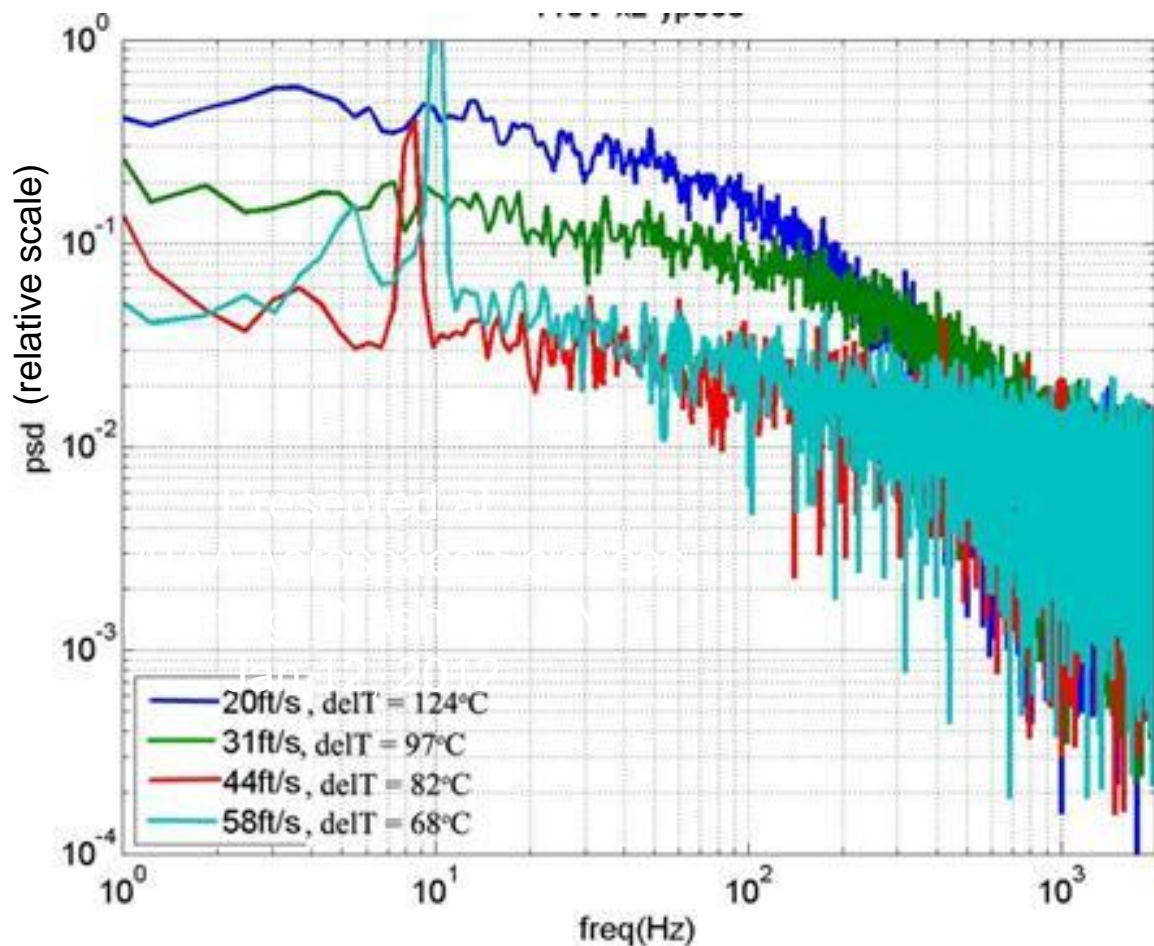
Heated flat plate in wind tunnel

Temperature distribution measured by an IR camera



- 60ft/s flow, ~600W heat flux on a 9"X12" plate
- Possible laminar separation due to sharp leading edge
- Currently modifying the leading edge to elliptical shape

Density fluctuation spectra from heated flat plate



- *Probe location: $x=2''$ from leading edge, $y=0.065''$ from plate surface.*

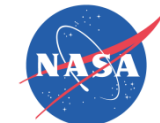
- vibration of Laser mount – spurious tones

- **Nevertheless, spectral levels rise by a factor of 100 over the noise floor**

Work in progress:

1. Reduce tunnel vibration
2. Detailed Survey of density spectra for boundary-layer transition
3. 2-point and multi-point space-time correlation of density fluctuations
4. Spectroscopic setup to measure temperature profiles

Summary



- Started from scratch - **first time setup at ARC**
 - Except for the laser, all optics and electronics were purchased, optical train designed, and implemented.
- Progressed towards two working setup:
 - Bench-top system around a clean jet
 - Working system to measure density fluctuations spectra
 - Work in progress: Spectroscopic setup to resolve Rayleigh spectra for velocity and temperature measurement
 - A low-speed wind tunnel setup
 - Overcame problems with aerosol contaminations, surface proximity
 - A two-PMT cross-correlation system and photo-electron counting was used for density fluctuations spectra
 - Spectra of density fluctuations show high signal-to-noise ratio: $10^2 - 10^4$
 - Work in progress – **Study boundary layer transition via density fluctuations – possible for the first time due to the present advancement**

We are thankful to the ARMD Seedling program to help “germinate” a new Rayleigh setup for wind tunnel applications.



Programmatic: Product & Deliverables

- Duration Feb. 2013 – Aug 2014 (6 month extension)
- Start – end TRL: 1- 4

• Products:

- (a) Hardware and software to measure density fluctuations spectra. Apr 2014✓
- (b) Preliminary hardware setup for spectroscopic analysis to perform velocity and temperature measurements. Aug 2014✓

• Deliverables and schedule:

- (a) Design of the Rayleigh system & component procurement Jun 2013✓
- (b) Proof-of-concept demonstration in a heated free-jet Aug 2013✓
- (c) Cleaning of a research wind tunnel in FML, verification of operation Feb 2014✓
- (d) Proof-of-concept demonstration in a subsonic wind tunnel at FML Apr 2014✓
- (e) Spectroscopic setup for velocity & temperature measurements Aug 2014
(in progress)

- **Forward support:** Effort continuing under Transformative Aeronautics Concepts Program (Tools and Methods)
 - Not part of this presentation